Basic information

Lectures       Tu/Th 14:00-15:20 PCYNH 120
Instructor     Prof. Alexis Akira Toda
Office hours  Tu/Th 13:00-14:00, ECON 211
Email          atoda@ucsd.edu
Webpage        https://sites.google.com/site/aatoda111/
(Teaching → Mathematical Economics)
TA              Miles Berg, Econ 128, mlberg@ucsd.edu (Office hours: TBD)

Course description

Carl Friedrich Gauss said mathematics is the queen of the sciences (and number theory
is the queen of mathematics). Paul Samuelson said economics is the queen of the social
sciences. Not surprisingly, modern economics is a highly mathematical subject.

Mathematical economics studies the mathematical foundations of economic theory
in the approach known as the Arrow-Debreu model of general equilibrium. Partial
equilibrium (things like demand and supply curves), which you have probably learned
in Econ 100ABC, considers each market separately. General equilibrium (GE for short),
on the other hand, considers the economy as a whole, taking into account the interaction
of all markets.

Econ 113 is probably the most mathematically advanced undergraduate course of-
fered at UCSD Economics, but it should have a high return. In the course, we will
develop a mathematical model of classical economic thoughts like Bentham’s “greatest
happiness principle” and Smith’s “invisible hand”, and prove theorems. Then we will
apply the theory to international trade, finance, social security, etc. Time permitting, I
will talk about my own research.

Prerequisites

A year of calculus and a year of upper division microeconomic theory (at UCSD these
courses are Math 20ABC and Economics 100ABC) are required. Students with very
strong mathematics preparation (typically including one quarter of real analysis, UCSD
Math 140A or 142A) may enroll without economics prerequisites. Certain ‘mathematical
maturity’ (familiarity with abstract thinking and manipulations of symbols instead of
concrete numbers) is helpful, but in my opinion you can acquire it only by self-study.

The required textbook for this course is [1], written by Prof. Ross Starr at UCSD, who has taught this course for many years. This book does not contain much examples but is self-contained and pedagogic in that it proceeds from the easy and special case to the difficult and general case. An added bonus is an accessible proof of the Brouwer fixed point theorem. [2] Chapters 1–7 is roughly the same level as [1], but contains lots of examples and exercises and thus may complement your study (though not required). Those who wish to pursue a Ph.D. in economics should get [3] [4], which are standard graduate-level texts. However, [3] may not be useful for learning due to its conciseness.

The course will use a lot of math, as the course title suggests. Relevant topics are basic linear algebra (but not much), calculus, convex analysis, and constrained optimization. For the last two topics, either [5] or my lecture notes for Econ 172B Operations Research (posted at my website) might be useful, but I will cover them briefly in class so you don’t need to study in advance.

Preliminary course outline

1. Introduction
2. Definition of Arrow-Debreu model
3. Crash course in convex analysis and convex programming
4. Quasi-linear model: mathematical formulation of Bentham’s “greatest happiness principle”
5. First and second welfare theorems: mathematical formulation of Smith’s “invisible hand”
6. Existence of equilibrium (correspondences, maximum theorem, Brouwer and Kakutani fixed point theorems)
7. Scope of markets, market failure, and prescriptions
8. International trade and comparative advantage
9. Capital asset pricing theory (CAPM)
10. Overlapping generations (OLG) model and social security
11. My own research

Assignments

There are no assignments for this course (because it is impossible to monitor you to do the assignments by yourselves). However, each lecture note will contain a few exercises, though typically at a higher level than the exam questions. In addition, you can download past exams from my personal website listed above, so make sure to check it out. Solve them by yourself: this is the best way to understand the material and to get prepared for the exams. Time permitting, we will go through the solution of some of the problems during the class.
Exams

There will be a quiz, a midterm, and a final. Please mark your calendar:

**Quiz** Tuesday October 18, in class

**Midterm** Thursday November 17, in class

**Final** Thursday December 8, 15:00–18:00, location TBA

The exam dates are non-negotiable. If you miss the quiz or the midterm for a documented, university approved reason (i.e., illness, family emergency, official university trip, etc.) the weight for that exam will be placed on the final. If you miss an exam for another reason (i.e., oversleep, vacation, etc.) you will receive a zero for that exam. No one will be allowed to start an exam after the first person leaves it. You are only permitted to use pens, pencils, and a straight edge (no calculator).

Grades

Each of the quiz, midterm, and final will be graded on a 0–100 scale. Your course grade will be determined by the formula

\[ G = 0.1 \max(Q, M) + 0.2 \max(M, F) + 0.7F, \]

where \(G\) is the course grade and \(Q, M, F\) are the scores on the quiz, midterm, and final. The course grade \(G\) will be converted to letter grades at my discretion at the end of the quarter. (So please don’t ask me questions like “What is the letter grade corresponding to \(x\) points in midterm?”)

As you can see from this formula, you are not required to take the quiz, since in theory you can still obtain a perfect course grade if \(Q = 0\) and \(M = F = 100\). The idea is that I would like to give you some feedback before the deadline to drop class without “W” grade. (For your information, each year the score of the first exam is a strong predictor of the course grade, and about 30% of students drop out after the first exam.)

Regrade requests must be made through a written statement before the start of class one week after the exam was first passed back. Extensions will only be permitted if you have a documented, university approved reason for missing the entire week after the exam was first passed back. If you request a regrade I reserve the right to regrade your entire exam and your score could go up, down, or stay the same. My regrade decision is final.

Questions

The best opportunity to ask questions is during the class, for two reasons. First, you can resolve your question immediately (assuming I know how to answer). Second, your classmates are likely to have similar questions, so they can benefit from questions being resolved and I benefit by saving time. If you have a question outside of class that cannot be resolved by Googling or discussing with your friends, please first ask your TA. If still unresolved, you can show up during my office hour listed above (no appointment necessary).
How to do well in this course

Get your favorite math text (linear algebra and calculus) or my lecture notes of Econ 172B at hand so that you can refer if necessary. Experience tells that (this is true) students who regularly attend classes outperform those who don’t, so come to class. Ask questions during the class whenever you don’t understand. Read the lecture notes. Solve exercises and past exams (posted at my web page) without looking at the solutions. If you do well in this course, you have a good chance to be admitted to a good Ph.D. program (and therefore get a lucrative job in the future). Let me know if you need a letter of recommendation.

Academic integrity

I take academic dishonesty seriously. Any student found guilty of academic dishonesty will earn a failing grade for the course. In addition to this sanction, the Council of Deans of Student Affairs will also impose a disciplinary penalty.

UCSD policy:  
http://senate.ucsd.edu/manual/appendices/appendix2.pdf

Facts about academic integrity:
http://students.ucsd.edu/academics/academic-integrity/facts.html

Consequences of cheating:
http://students.ucsd.edu/academics/academic-integrity/consequences.html

References


